

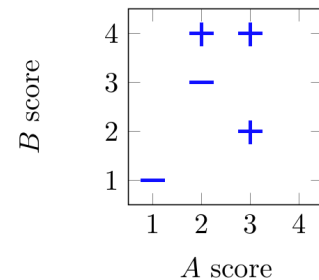
Artificial Intelligence II

Exercise 9

Q1. Perceptron

You want to predict if movies will be profitable based on their screenplays. You hire two critics A and B to read a script you have and rate it on a scale of 1 to 4. The critics are not perfect; here are five data points including the critics' scores and the performance of the movie:

#	Movie Name	A	B	Profit?
1	Pellet Power	1	1	-
2	Ghosts!	3	2	+
3	Pac is Bac	2	4	+
4	Not a Pizza	3	4	+
5	Endless Maze	2	3	-



1. First, you would like to examine the linear separability of the data. Plot the data on the 2D plane above label profitable movies with + and non-profitable movies with - and determine if the data are linearly separable.

Solution:

The data are linearly separable.

2. Now you decide to use a perceptron to classify your data. Suppose you directly use the scores given above as features, together with a bias feature. That is $f_0 = 1$, $f_1 =$ score given by A and $f_2 =$ score given by B.

Run one pass through the data with the perceptron algorithm, filling out the table below. Go through the data points in order, e.g. using data point #1 at step 1.

step	Weights	Score	Correct?
1	$[-1, 0, 0]$	$-1 \cdot 1 + 0 \cdot 1 + 0 \cdot 1 = -1$	yes
2	$[-1, 0, 0]$	$-1 \cdot 1 + 0 \cdot 3 + 0 \cdot 2 = -1$	no
3	$[0, 3, 2]$	$0 \cdot 1 + 3 \cdot 2 + 2 \cdot 4 = 14$	yes
4	$[0, 3, 2]$	$0 \cdot 1 + 3 \cdot 3 + 2 \cdot 4 = 17$	yes
5	$[0, 3, 2]$	$0 \cdot 1 + 3 \cdot 2 + 2 \cdot 3 = 12$	no

Final weights:

Solution:

$[-1, 1, -1]$

3. Have weights been learned that separate the data?

Solution:

With the current weights, points will be classified as positive if $-1 \cdot 1 + 1 \cdot A + -1 \cdot B \geq 0$, or $A - B \geq 1$. So we will have incorrect predictions for data points 3:

$$-1 \cdot 1 + 1 \cdot 2 + -1 \cdot 4 = -3 < 0$$

and 4:

$$-1 \cdot 1 + 1 \cdot 3 + -1 \cdot 4 = -2 < 0$$

Note that although point 2 has $w \cdot f = 0$, it will be classified as positive (since we classify as positive if $w \cdot f \geq 0$).

4. More generally, irrespective of the training data, you want to know if your features are powerful enough to allow you to handle a range of scenarios. Circle the scenarios for which a perceptron using the features above can indeed perfectly classify movies which are profitable according to the given rules:

- (a) Your reviewers are awesome: if the total of their scores is more than 8, then the movie will definitely be profitable, and otherwise it won't be.

Solution:

Can classify (consider weights $[-8, 1, 1]$)

- (b) Your reviewers are art critics. Your movie will be profitable if and only if each reviewer gives either a score of 2 or a score of 3.

Solution:

Cannot classify

- (c) Your reviewers have weird but different tastes. Your movie will be profitable if and only if both reviewers agree.

Solution:

Cannot classify